

D:  $(-\infty, \infty)$  R:  $(0, \infty)$

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\*Inverse of each other

$$\log_e x = \ln x$$

$$\log_b A = e \leftrightarrow b^e = A$$

b is base, e is exponent, A is answer

$$\ln A = x \leftrightarrow e^x = A$$

EXAMPLE:  $\ln(x+4)$  inverse:  $e^x - 4$  \*left to down

EXAMPLE:  $\ln x + 4$  inverse:  $e^{x-4}$  \*up to right

Horizontal and vertical shifts switch and change the sign

\*D and R switch.

- 1) Use the given function  $f$  to answer parts (a) through (c).

$$f(x) = \ln(x - 3)$$

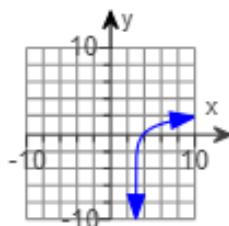
- (a) Find the domain of  $f$ .

The domain of  $f$  is  $(3, \infty)$ .

(Type your answer in interval notation.)

- (b) Graph  $f$ . Choose the correct graph below.

Right 3



- (c) From the graph, determine the range and an asymptote of  $f$ .

The range of  $f$  is  $(-\infty, \infty)$ .

(Type your answer in interval notation.)

Determine the vertical asymptote of  $f$ . Select the answer box to complete your choice.

Ⓐ The vertical asymptote of  $f$  is  $x = 3$ .

- (d) Find  $f^{-1}$ , the inverse of  $f$ .

$$f^{-1}(x) = e^x + 3 \quad (\text{Simplify your answer.})$$

- (e) Find the domain and range of  $f^{-1}$ .

The domain of  $f^{-1}$  is  $(-\infty, \infty)$ .

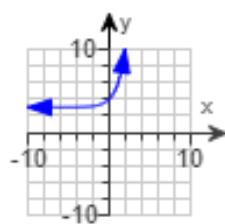
(Type your answer in interval notation.)

The range of  $f^{-1}$  is  $(3, \infty)$ .

(Type your answer in interval notation.)

- (f) Graph  $f^{-1}$ . Choose the correct graph below.

Up 3



- 2) Begin with the graph of  $y = e^x$ . Use transformations to graph the function below. Then determine its domain, range, and horizontal asymptote.

$$f(x) = 9 - e^{-x}$$

Check reflection for both FIRST

What is the domain of  $f(x) = 9 - e^{-x}$ ?

$$(-\infty, \infty)$$

(Type your answer in interval notation.)

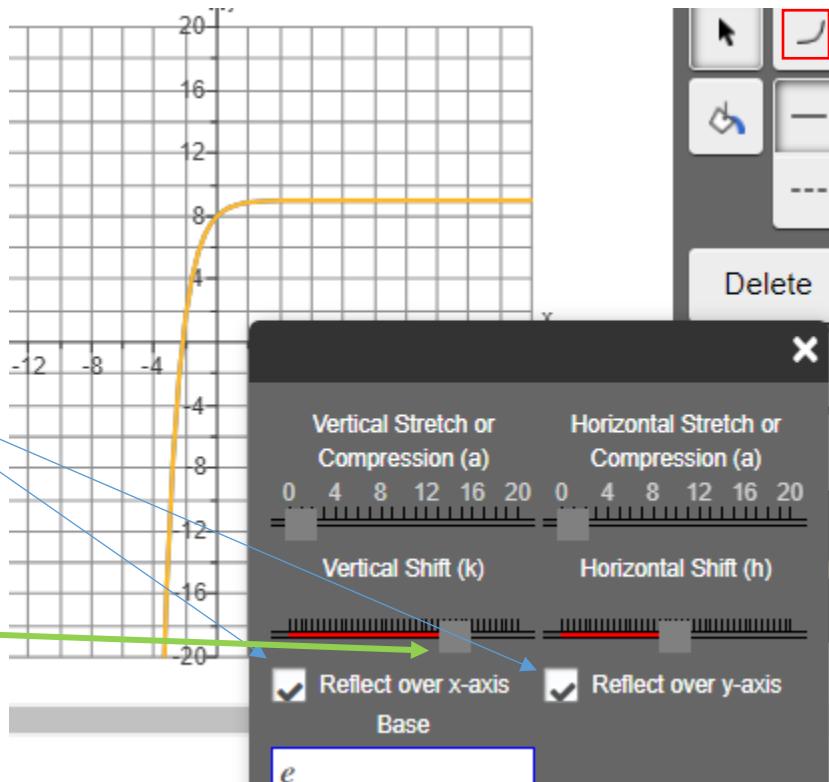
What is the range of  $f(x) = 9 - e^{-x}$ ?

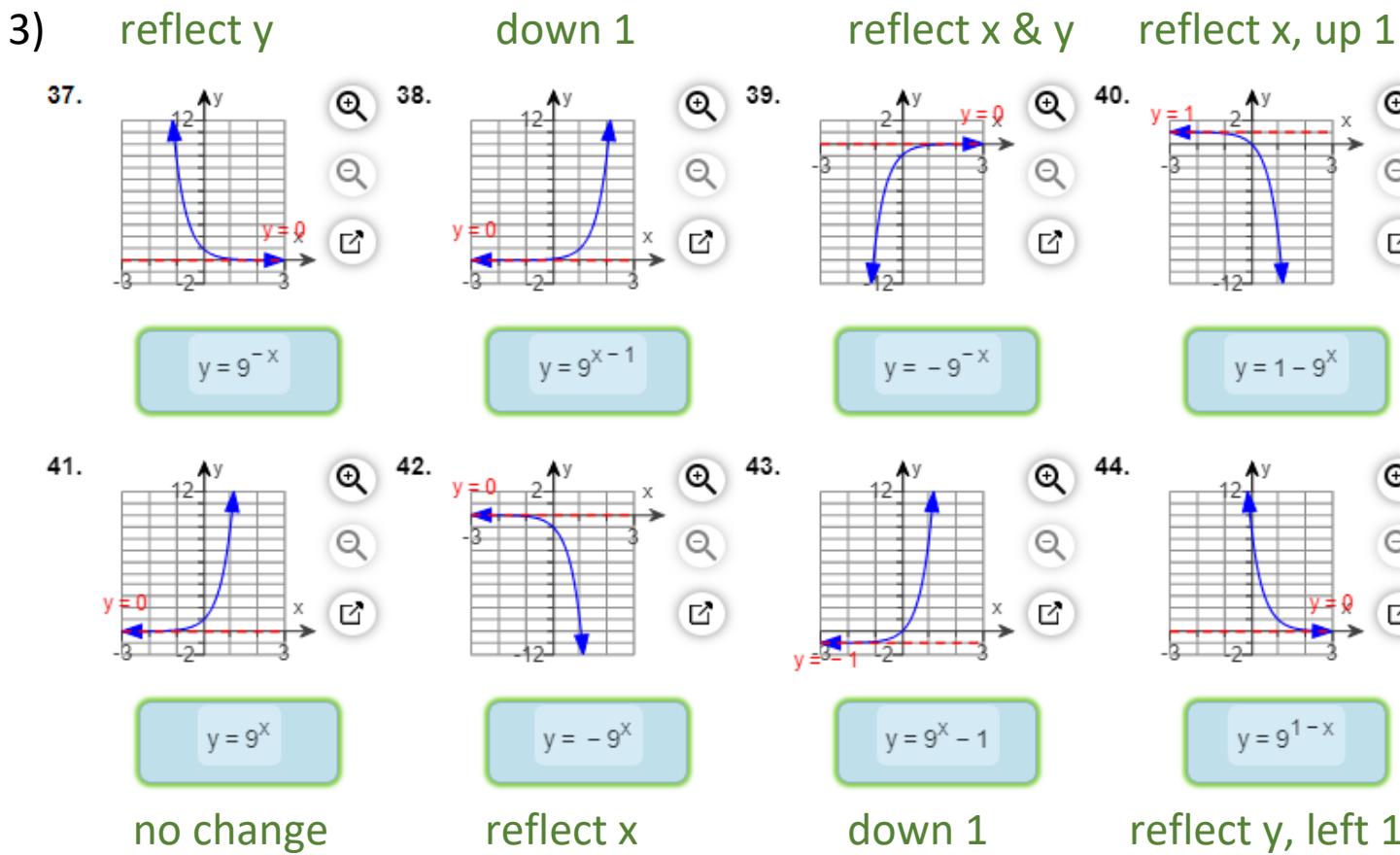
$$(-\infty, 9)$$

(Type your answer in interval notation.)

What is the horizontal asymptote of  $f(x) = 9 - e^{-x}$ ?

$$y = 9$$





4) Solve the equation.

$$\left(\frac{2}{5}\right)^x = \left(\frac{8}{125}\right) \quad 2^3 = 8 \text{ and } 5^3 = 125 \text{ then } x = 3$$

- 5) Determine whether the function given by the table is linear, exponential, or neither. If the function is linear, find a linear function that models the data; if it is exponential, find an exponential function that models the data.

x	f(x)
-1	$\frac{1}{6}$
0	1
1	6
2	36
3	216

- A. The function is exponential. An exponential function that models the data is  $f(x) = 6^x$  (Simplify your answer.)

- 6) Change the logarithmic statement to an equivalent statement involving an exponent.

$$\log_a 3 = 5$$

The equivalent exponential statement is  $a^5 = 3$ . (Type an equation.)

- 7) Find the domain of the function.

$$h(x) = 6 - 8 \log_5 \left[ \frac{x}{8} - 2 \right]$$

only solve inside [ ]

$$\frac{x}{8} - 2 = 0 \quad x = 16$$

The domain of  $h$  is  $(16, \infty)$ .

(Type your answer in interval notation.)

- 8) Use transformations to graph the function. Determine the domain, range, horizontal asymptote, and  $y$ -intercept of the function.

$$f(x) = 3^{-x} - 4$$

What is the domain of  $f(x) = 3^{-x} - 4$ ?

$$(-\infty, \infty)$$

(Type your answer in interval notation.)

What is the range of  $f(x) = 3^{-x} - 4$ ?

$$(-4, \infty)$$

(Type your answer in interval notation.)

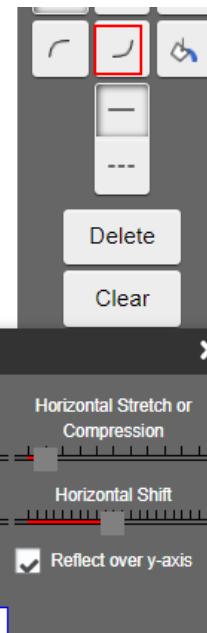
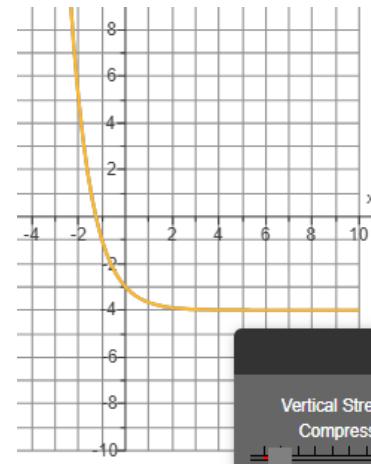
Determine the horizontal asymptote of  $f(x) = 3^{-x} - 4$ . Select the correct choice below and, if necessary, fill in the answer box(es) to complete your choice.

- B. The function has one horizontal asymptote,  $y = -4$ .

(Type an equation.)

What is the  $y$ -intercept of  $f(x) = 3^{-x} - 4$ ?

3 (Type an integer or a simplified fraction.)



reflect across  $y$ , down 4

- 9) Find the exact value of the logarithm without using a calculator.

$$\log_{1/2} 512 \quad \frac{1}{2}x = 512 \quad 2^9 = 512 \quad x = -9$$

$\frac{1}{2}$  to 2 is negative exponent

- 10) Solve the equation.

$$\log_x 9 = 2$$

$$x^2 = 9$$

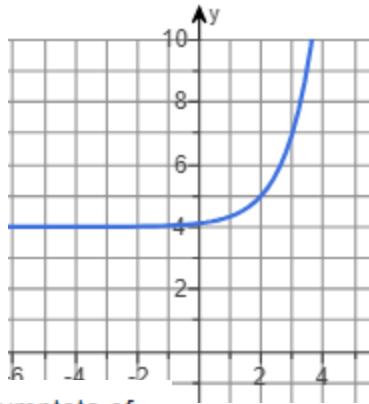
$$x = 3$$

$b^0 = 1$	$x^{-1} = \frac{1}{x}$	$x^{1/2} = \sqrt{x}$
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- 11) Use transformations to graph the function.  
Determine the domain, range,  
horizontal asymptote, and  $y$ -intercept of the  
function.

$$f(x) = 4 + 3^{x-2}$$

Right 2, up 4



What is the domain of  $f(x) = 4 + 3^{x-2}$ ?

( $-\infty, \infty$ )

(Type your answer in interval notation.)

What is the range of  $f(x) = 4 + 3^{x-2}$ ?

(4,  $\infty$ )

(Type your answer in interval notation.)

Determine the horizontal asymptote of  
 $f(x) = 4 + 3^{x-2}$ . Select the correct choice  
below and, if necessary, fill in the  
answer box(es) to complete your choice.

- A. The function has one  
horizontal asymptote,  $y = 4$ .  
(Type an equation.)

- 12) Determine whether the function given by the table is linear, exponential, or neither. If the function is linear, find a linear function that models the data; if it is exponential, find an exponential function that models the data.

x	f(x)
-1	9
0	8
1	9
2	72
3	576
4	4608

- B. The function is exponential. An exponential function that models the data is  $f(x) = 9 \cdot 8^x$ .  
(Simplify your answer.)