

1) $18 - 3x \geq 6$

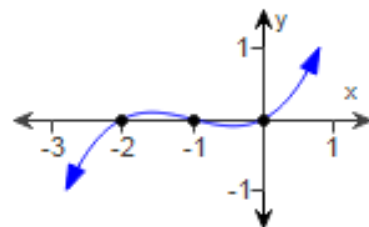
- $3x \geq -12$ switch the sign when dividing by negative #

$x \leq 4$ $\{x \mid x \leq 4\}$ or $(-\infty, 4]$

2) Use the graph of the function f to solve the inequality.

(a) $f(x) > 0$ $(-2, -1) \cup (0, \infty)$

(b) $f(x) \leq 0$ $(-\infty, -2] \cup [-1, 0]$



a) *since it is $>$, it does not include the point on the x-axis parenthesis

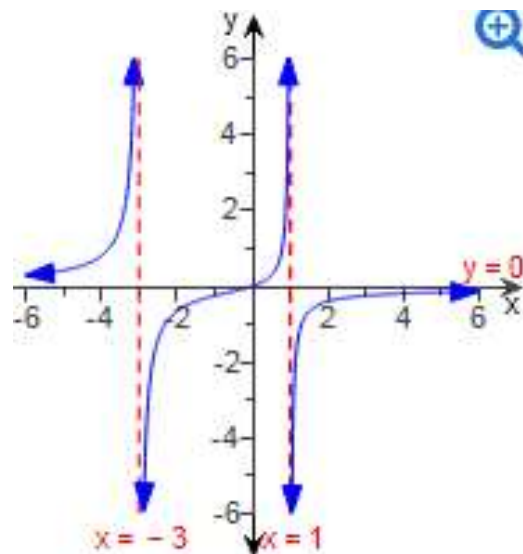
b) *since it is \leq , it does include the point on the x-axis brackets

3)

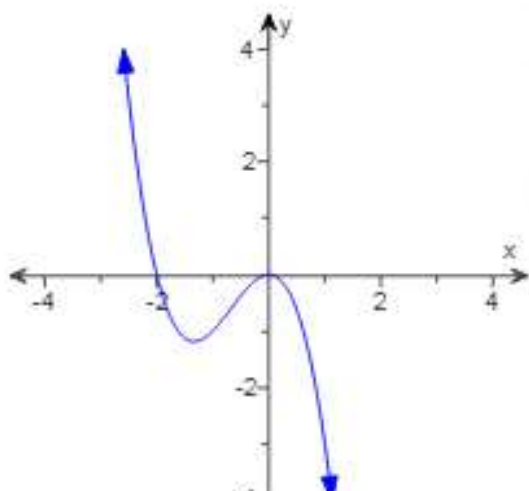
Use the graph of the function f to solve the inequality.

(a) $f(x) < 0$ $(-3, 0) \cup (1, \infty)$

(b) $f(x) \geq 0$ $(-\infty, -3) \cup [0, 1]$



4)

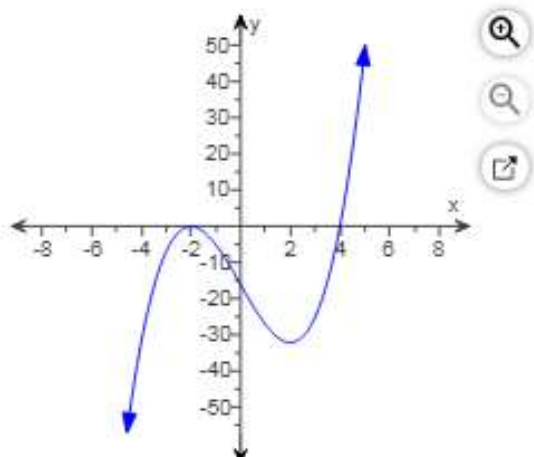
Solve the inequality $f(x) < 0$, where $f(x) = -x^2(x + 2)$, by using the graph of the function.

$(-2, 0) \cup (0, \infty)$

since it is $<$, it does not include the point on the x-axis

Solve the inequality $f(x) \leq 0$, where $f(x) = (x - 4)(x + 2)^2$, by using the graph of the function.

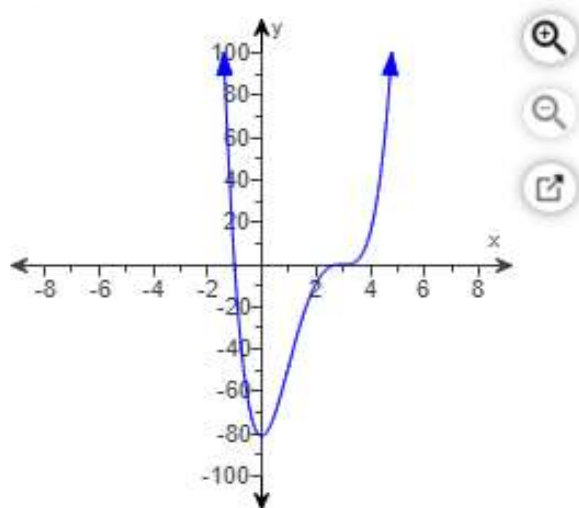
5)



$$(-\infty, 4]$$

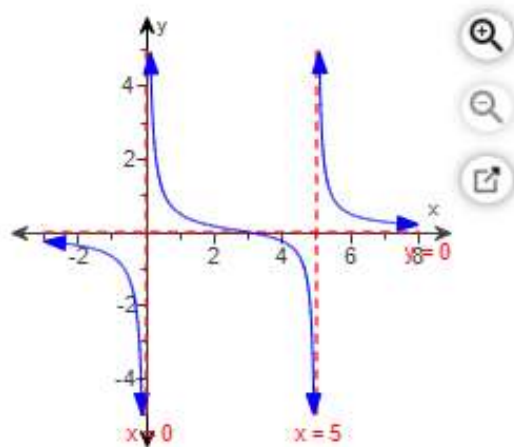
since it is \leq , it includes x-axis

6) Solve the inequality $f(x) \geq 0$, where $f(x) = 3(x + 1)(x - 3)^3$, by using the graph of the function.



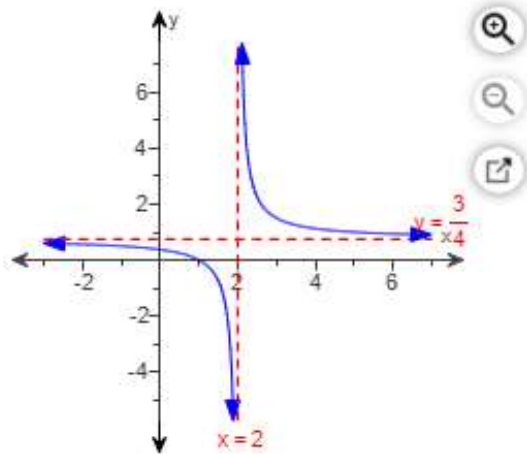
$$(-\infty, -1] \cup [3, \infty)$$

7) Solve the inequality $R(x) < 0$, where $R(x) = \frac{x - 3}{x(x - 5)}$, by using the graph of the function.



$$(-\infty, 0) \cup (3, 5)$$

- 8) Solve the inequality $R(x) \leq 0$, where $R(x) = \frac{3x-3}{4x-8}$, by using the graph of the function.



[1,2)

- 9) Solve the inequality algebraically.

$$(x-9)^2(x+5) < 0$$

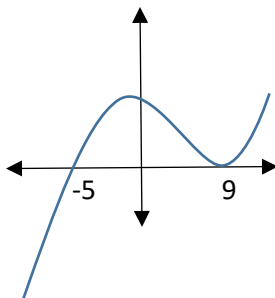
Intercepts are -5 and 9

List the intervals and sign in each interval. Complete the following table.
(Type your answers in interval notation. Use ascending order.)



Interval	$(-\infty, -5)$	$(-5, 9)$	$(9, \infty)$
Sign	Negative	Positive	Positive

*easiest to make a graph of x^3 that touches at 9 crosses at -5



Use this graph to fill in the positive or negative in the chart

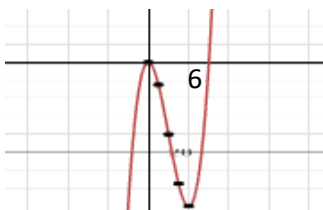
We are looking for below the x-axis since it is < 0

$(-\infty, -5)$

- 10) Solve the inequality $x^3 - 6x^2 > 0$ *factor first*

$$x^2(x-6) > 0 \quad \text{x-intercepts are 0 and 6}$$

*easiest to make a graph of x^3 that touches at 0 and crosses at 6

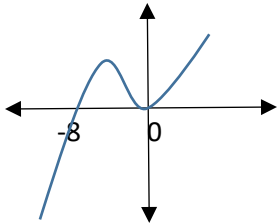


We are looking for above the x-axis since it is > 0

$(6, \infty)$

11) Solve the inequality $3x^3 > -24x^2$ $3x^3 + 24x^2 > 0$ *factor first*
 $3x^2(x+8) > 0$ *x-intercepts are 0 and -8*

**easiest to make a graph of x^3 that touches at 0 and crosses at -8*



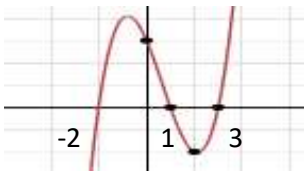
Interval	$(-\infty, -8)$	$(-8, 0)$	$(0, \infty)$
Sign	Negative	Positive	Positive

*We are looking for above the x-axis since it is > 0
open circle at 0*

$$(-8, 0) \cup (0, \infty)$$

12) Solve the inequality $(x-3)(x-1)(x+2) \geq 0$ *x-intercepts are -2, 1 and 3*

**easiest to make a graph of x^3 that crosses at -2, 1, 3*



We are looking for above the x-axis since it is ≥ 0

$$[-2, 1] \cup [3, \infty)$$

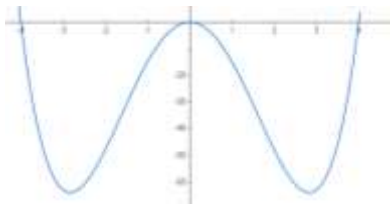
13) Solve the inequality $x^4 > 16x^2$ *solve first then factor*

$$x^4 - 16x^2 > 0$$

$$x^2(x^2 - 16) > 0$$

$$x^2(x+4)(x-4) > 0$$
 x-intercepts are -4, 0 and 4

**easiest to look at the graph of x^4 and touches at 0 crosses at -4 and 4*



We are looking for above the x-axis since it is > 0

$$(-\infty, -4) \cup (4, \infty)$$

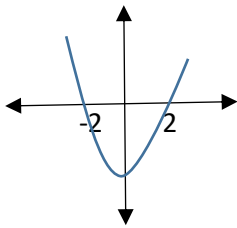
14) Solve the inequality $x^4 > 16$ *solve first then factor*

$$x^4 - 16 > 0$$

$$(x^2 - 4)(x^2 + 4) > 0$$

$$(x-2)(x+2)(x^2+4) > 0$$
 x-intercepts are -2, 2

**easiest to look at the graph of x^4 and crosses at -2 and 2*



We are looking for above the x-axis since it is > 0

$$(-\infty, -2) \cup (2, \infty)$$

FRACTIONAL INEQUALITIES

MAKE A NUMBER LINE

\geq means



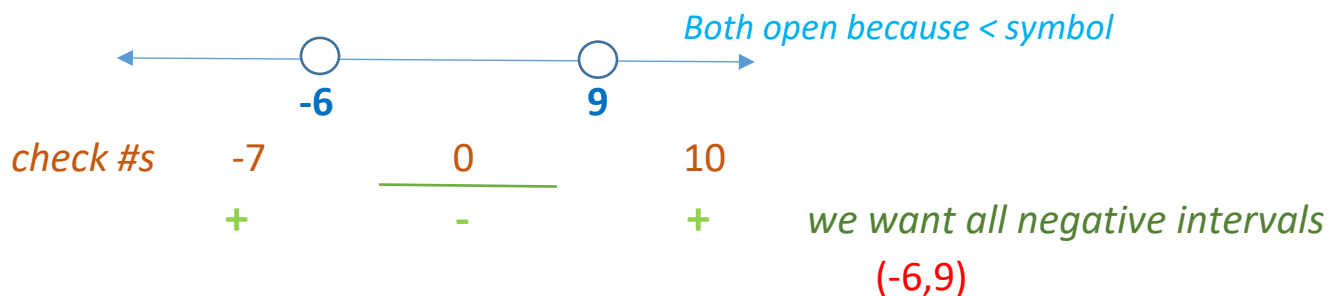
$>$ means



all values on bottom are

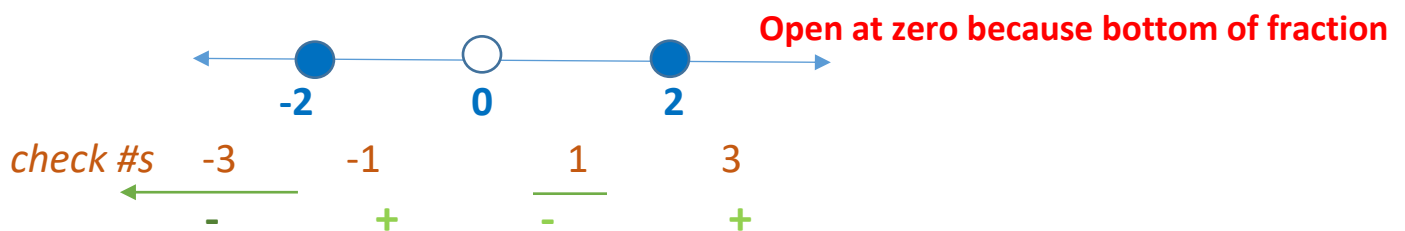
15) Solve the inequality $\frac{x+6}{x-9} < 0$ open circles from $<$

*we check all the critical points on a number line $x = -6, 9$



16) Solve the inequality $\frac{(x-2)(x+2)}{x} \leq 0$ closed circles from \leq

*we check all the critical points on a number line $x = -2, 0, 2$



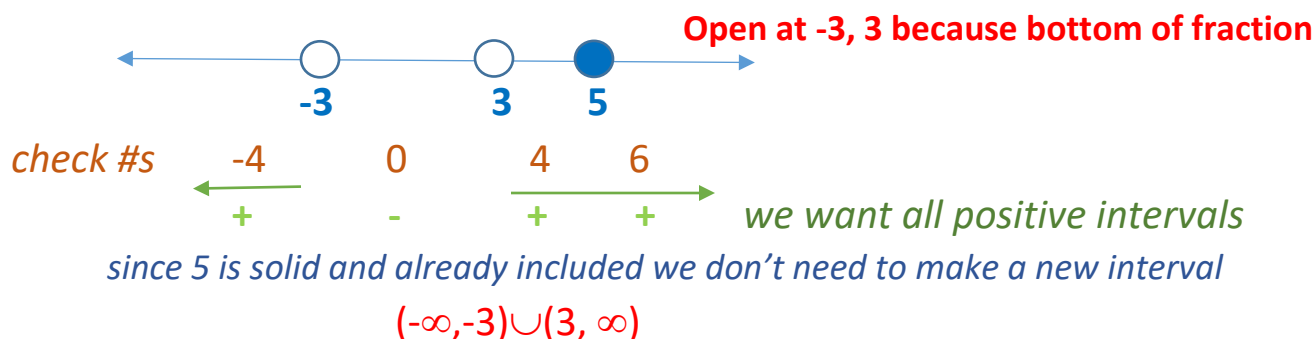
Interval	$(-\infty, -2)$	$(-2, 0)$	$(0, 2)$	$(2, \infty)$
Sign	Negative	Positive	Negative	Positive

we include the points and use negative intervals

$$(-\infty, -2] \cup (0, 2]$$

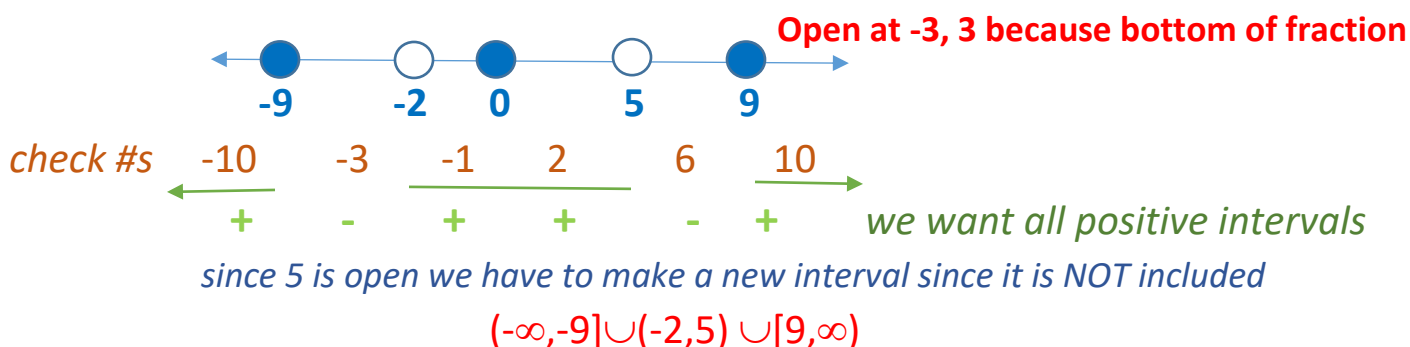
17) Solve the inequality $\frac{(x-5)^2}{x^2-9} \geq 0$ closed circles from \geq

*we check all the critical points on a number line $x = -3, 3, 5$



18) Solve the inequality $\frac{x^2(9+x)(x-9)}{(x+2)(x-5)} \geq 0$ closed circles from \geq

*we check all the critical points on a number line $x = -9, -2, 0, 5, 9$

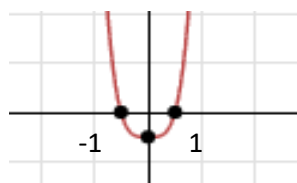


19) Solve the inequality $\sqrt{x^4 - 1}$ square root means $x \geq 0$

$$(x^2-1)(x^2+1)$$

$$(x-1)(x+1)(x^2+1)$$

*easiest to look at the graph of x^4 and crosses at -1, 1



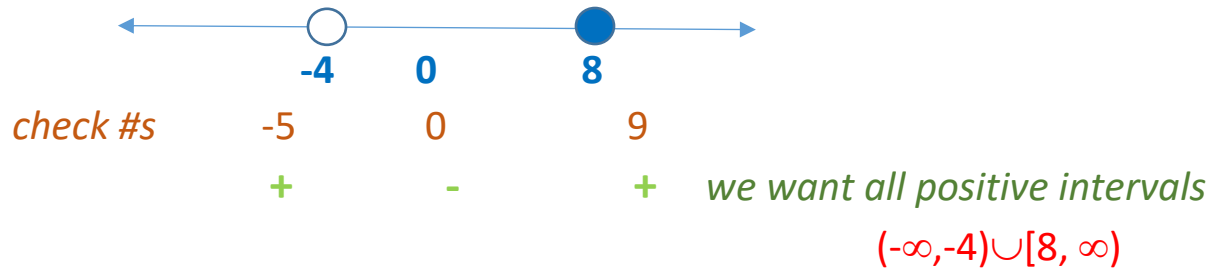
We are looking for above and include the x-axis since it is ≥ 0

$$(-\infty, -1] \cup [1, \infty)$$

20) Solve the inequality $\sqrt{\frac{x-8}{x+4}}$

square root is $x \geq 0 \rightarrow$ bottom cannot = 0; **Open at -4 because bottom of fraction**


*we check all the critical points on a number line $x = -4, 8$



21) Solve the quadratic inequality. Give the solution set in interval notation.

$$(x + 8)^2 \leq 0$$

Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

-  A. The solution set is the single point $\{-8\}$.
(Type an integer or a simplified fraction.)

EXTRA EXAMPLES:

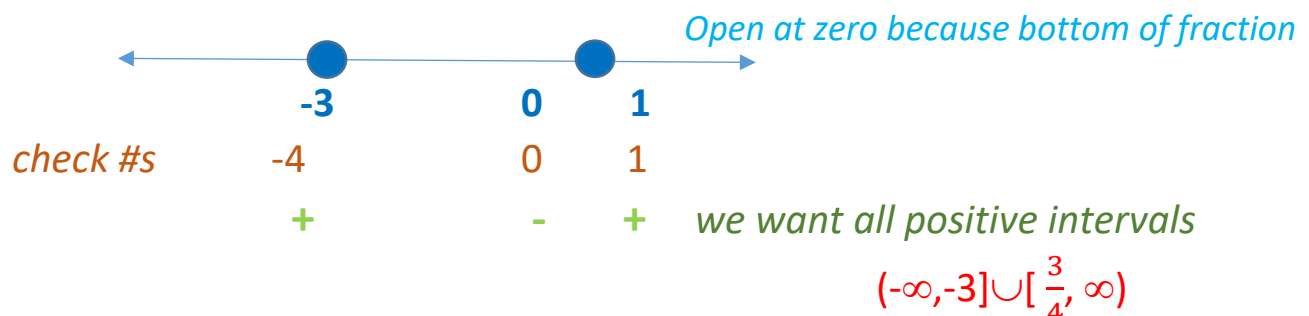
a) Solve the inequality $9x - 9 \geq -4x^2$

$$4x^2 + 9x - 9 \geq 0 \text{ use slide and divide}$$

$$x^2 + 9x - 36$$

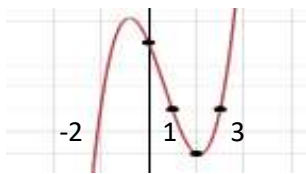
$(x + 12)(x - 3)$ divide by 4 $x = -3, \frac{3}{4}$

*we check all the critical points on a number line $x = 3, -\frac{3}{4}$



b) Solve the inequality $(x-3)(x-1)(x+2) > 0$

*easiest to look at the graph of x^3 and crosses at -2, 1, 3



We are looking for above the x-axis since it is > 0

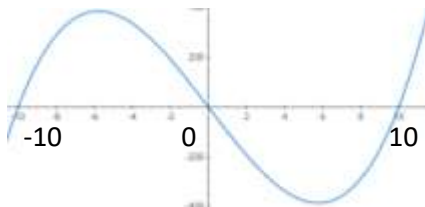
$$(-2, 1) \cup (3, \infty)$$

c) Solve the inequality $x^3 - 100x \leq 0$

$$x(x^2 - 100) \leq 0$$

$$x(x-10)(x+10) \leq 0$$

*easiest to look at the graph of x^3 and crosses at -10, 0, 10

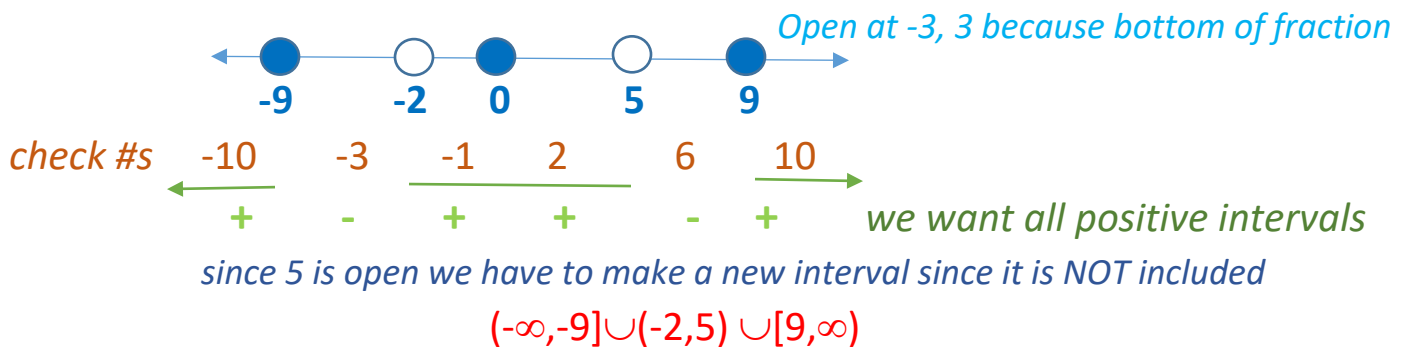


We are looking for below and include the x-axis since it is ≤ 0

$$(-\infty, -10] \cup [0, 10]$$

d) Solve the inequality $\frac{x^2(9+x)(x-9)}{(x+2)(x-5)} \geq 0$

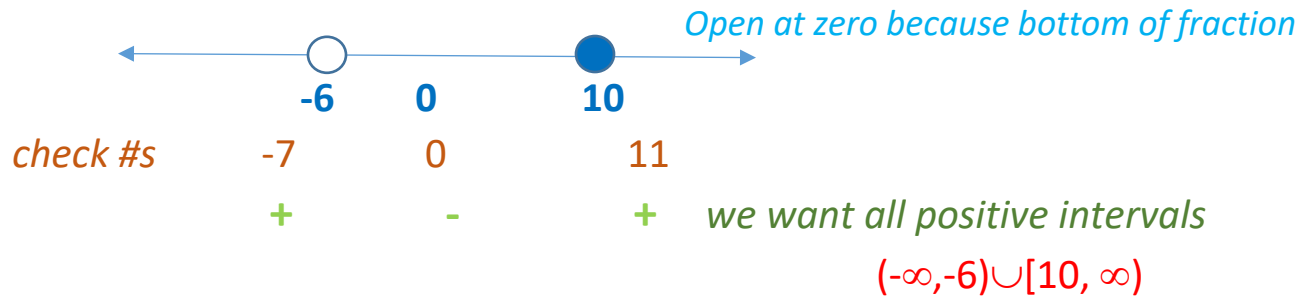
*we check all the critical points on a number line $x = -9, -2, 0, 5, 9$



e) Solve the inequality $\sqrt{\frac{x-10}{x+6}}$

square root means $x \geq 0$ but bottom cannot = 0 so bottom $x > 0$ and top $x \geq 0$

**we check all the critical points on a number line $x = -6, 10$*

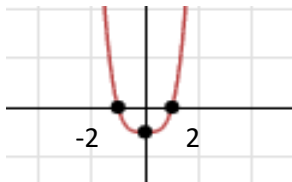


f) Solve the inequality $\sqrt{x^4 - 16}$ *square root means $x \geq 0$*

$$(x^2 - 4)(x^2 + 4)$$

$$(x - 2)(x + 2)(x^2 + 1)$$

**easiest to look at the graph of x^4 and crosses at -2, 2*

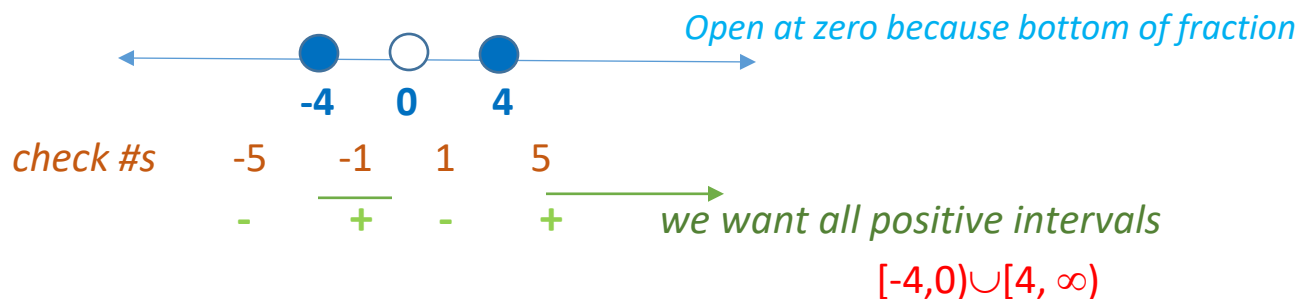


We are looking for above and include the x-axis since it is ≥ 0

$$(-\infty, -2] \cup [2, \infty)$$

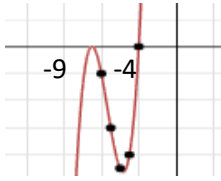
g) Solve the inequality $\frac{(x-4)(x+4)}{x} \geq 0$

**we check all the critical points on a number line $x = -4, 0, 4$*



h) Solve the inequality $(x+9)^2(x+4) < 0$ *x-intercepts are -9 and -4*

**easiest to make a graph of x^3 that touches at -9 crosses at -4*



We are looking for below the x-axis since it is < 0

$$(-\infty, -9) \cup (-9, -4)$$